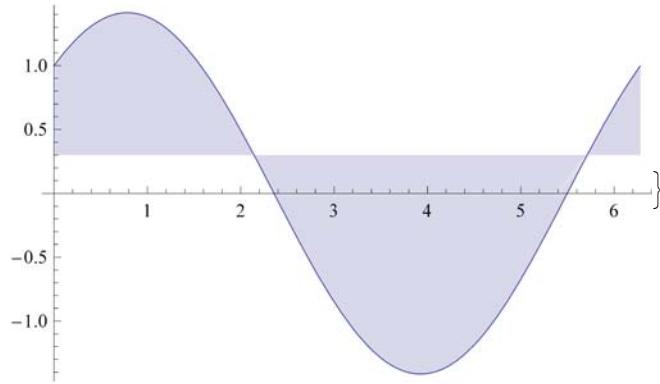
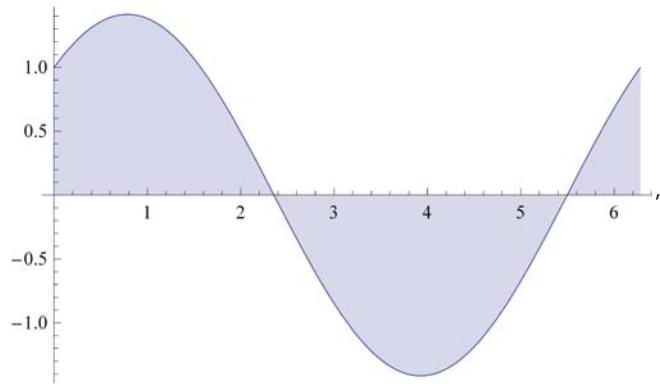
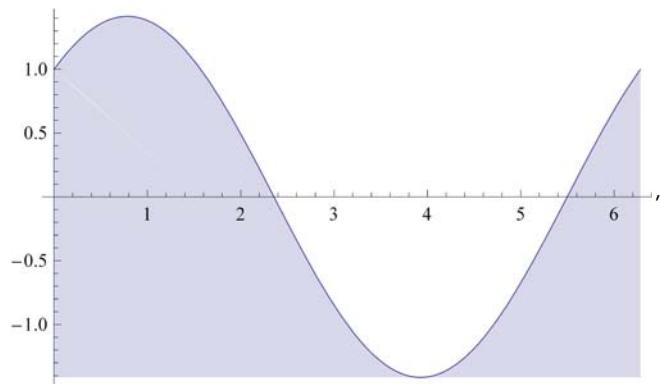
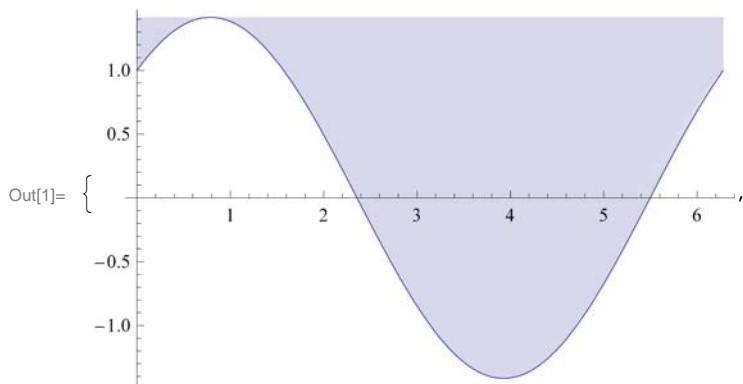


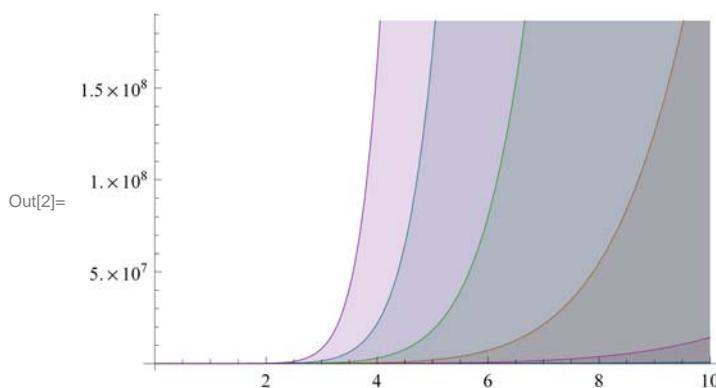
## **Filling**

is an option for `ListPlot`, `Plot`, `Plot3D` and related functions which specifies what filling to add under points, curves and surfaces.

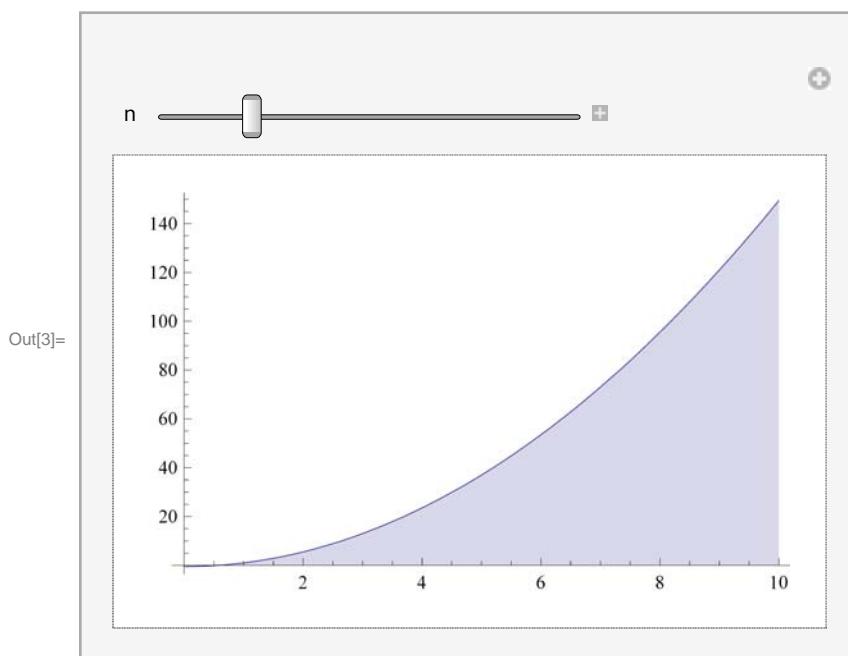
```
In[1]:= Table[Plot[Sin[x] + Cos[x], {x, 0, 2 Pi}, Filling -> f], {f, {Top, Bottom, Axis, 0.3}}]
```



In[2]:= Plot[Evaluate[Table[LegendreP[n, x], {n, 10}]], {x, 0, 10}, Filling → Axis]



In[3]:= Manipulate[Plot[LegendreP[n, x], {x, 0, 10}, Filling → Axis], {n, 0, 10, 1}]



**PDF**[*dist*, *x*] gives the probability density function for the symbolic distribution *dist* evaluated at *x*.

For continuous distributions, **PDF** [*dist*, *x*] *dx* gives the probability that an observed value will lie between *x* and *x* + *dx* for infinitesimal *dx*.

For discrete distributions, **PDF** [*dist*, *x*] gives the probability that an observed value will be *x*.

**PDF**[*dist*] gives the PDF as a pure function.

### NormalDistribution[ $\mu$ , $\sigma$ ]

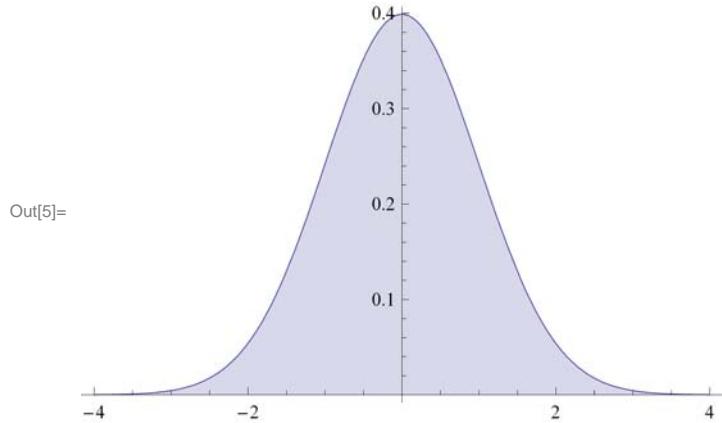
represents a normal (Gaussian) distribution with mean  $\mu$  and standard deviation  $\sigma$ .

The probability density for value *x* in a normal distribution is proportional to  $e^{-(x-\mu)^2/(2\sigma^2)}$ .

```
In[4]:= PDF[NormalDistribution[0, 2], x]
```

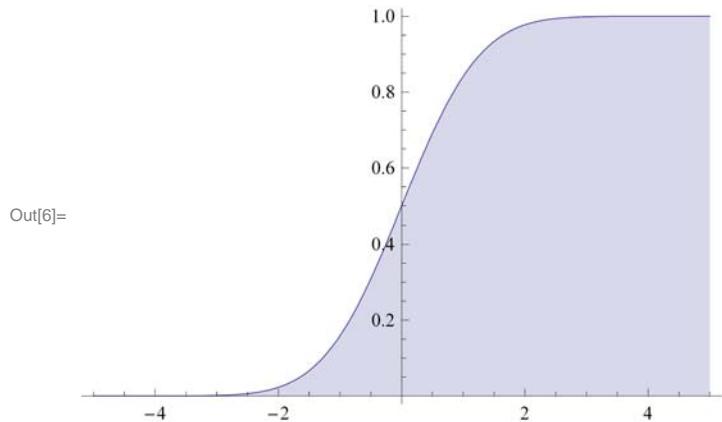
$$\text{Out}[4]= \frac{e^{-\frac{x^2}{8}}}{2 \sqrt{2 \pi}}$$

```
In[5]:= Plot[PDF[NormalDistribution[0, 1], x], {x, -4, 4}, Filling -> Axis]
```

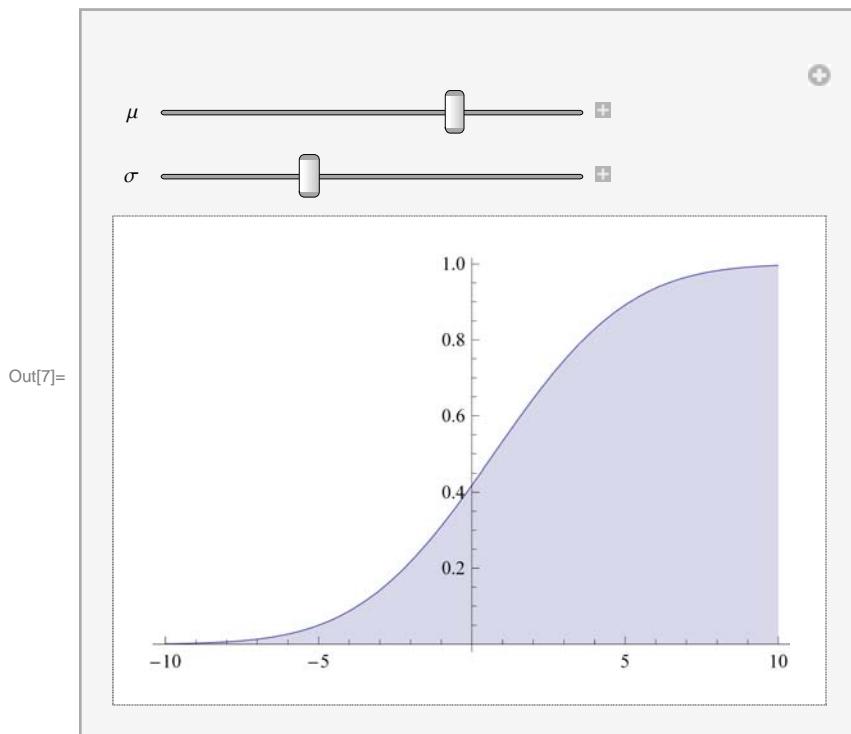


Plot the cumulative distribution function of the random variable:

```
In[6]:= Plot[CDF[NormalDistribution[0, 1], x], {x, -5, 5}, Filling -> Axis]
```

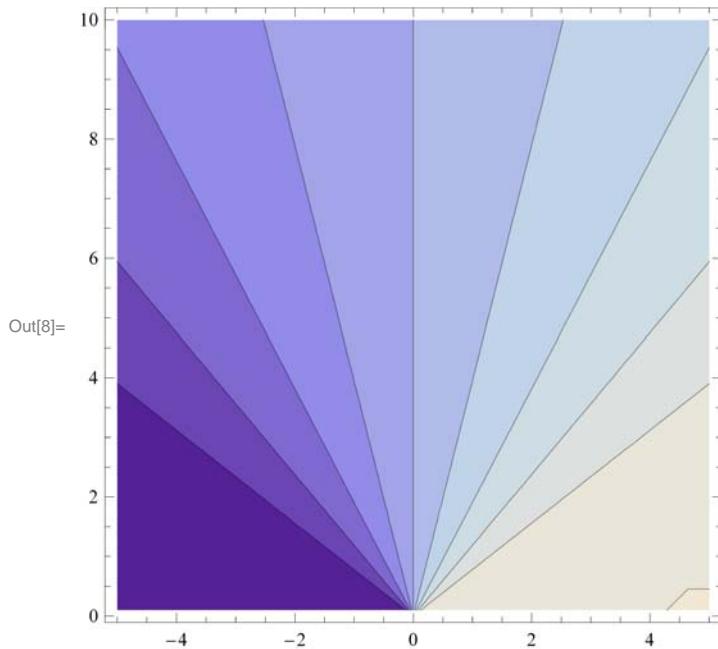


```
In[7]:= Manipulate[Plot[CDF[NormalDistribution[μ, σ], x], {x, -10, 10}, Filling -> Axis], {μ, 0, 1}, {σ, 1/10, 10}]
```



A contour plot as both  $x$  and  $\sigma$  are varied:

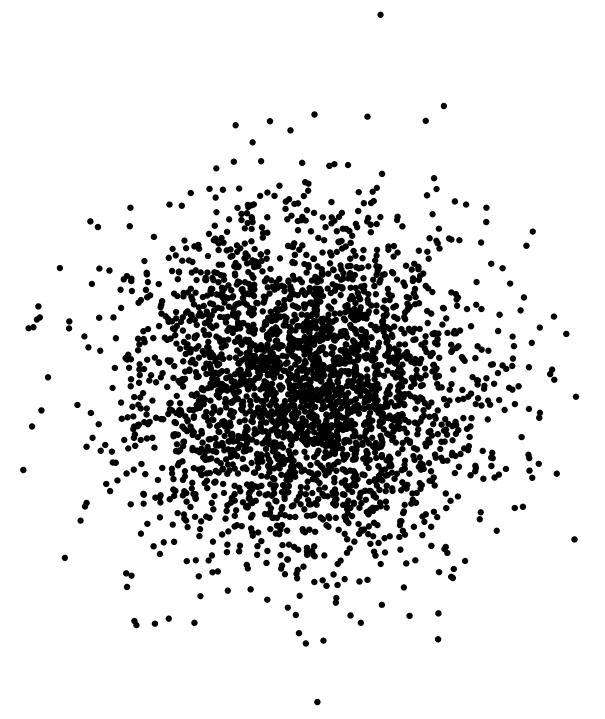
```
In[8]:= ContourPlot[
  CDF[NormalDistribution[0, σ], x], {x, -5, 5}, {σ, 1/10, 10}]
```



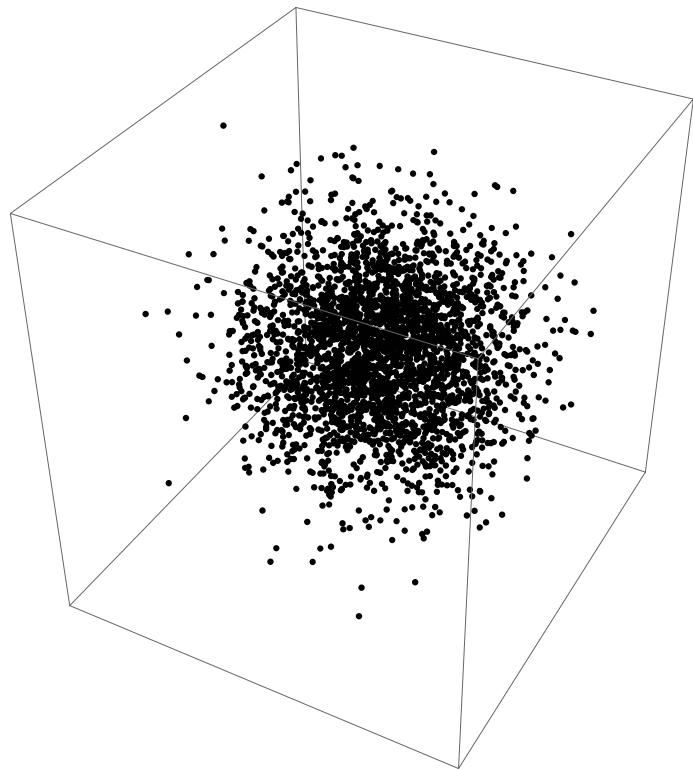
Normally distributed points in the plane and normally distributed points in 3D:

```
In[9]:= Graphics[Point[RandomReal[NormalDistribution[], {3000, 2}]]]
Graphics3D[Point[RandomReal[NormalDistribution[], {3000, 3}]]]
```

Out[9]=



Out[10]=

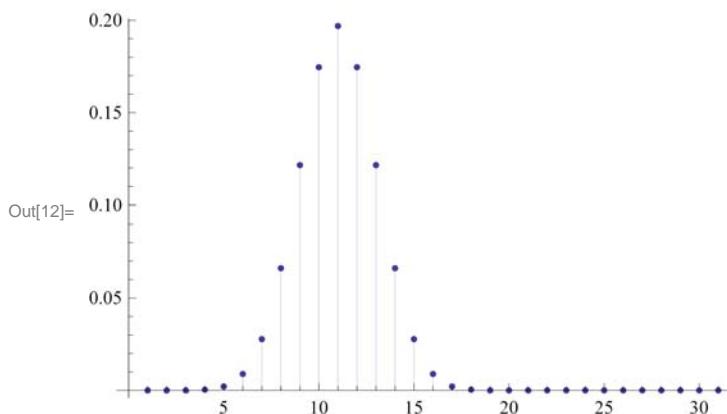


**A hypergeometric distribution** gives the distribution of the number of successes in  $n$  draws from a population of size  $n_{tot}$  containing  $n_{succ}$  successes.

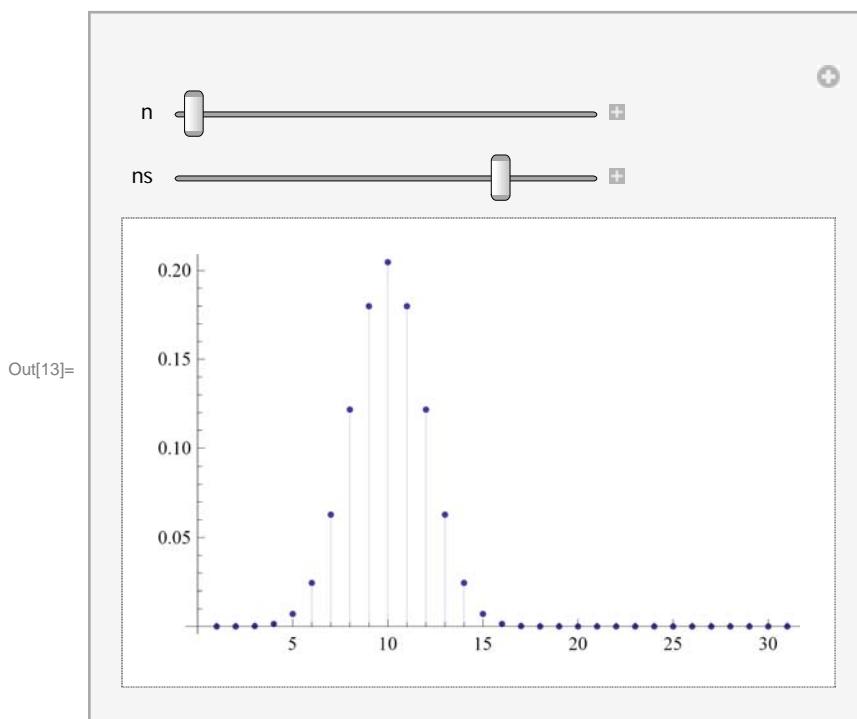
```
In[11]:= PDF[HypergeometricDistribution[1 n, nsucc, ntotal], k]
```

$$\text{Out}[11]= \frac{\text{Binomial}[nsucc, k] \text{Binomial}[-nsucc + ntotal, -k + n]}{\text{Binomial}[ntotal, n]}$$

```
In[12]:= ListPlot[Table[PDF[HypergeometricDistribution[50, 20, 100], k], {k, 0, 30}], Filling -> Axis]
```



```
In[13]:= Manipulate[ListPlot[Table[PDF[HypergeometricDistribution[5 n, ns, 100], k], {k, 0, 30}], Filling -> Axis], {n, 10, 50, 10}, {ns, 10, 20, 2}]
```



### PoissonDistribution[μ]

represents a Poisson distribution with mean  $\mu$ .

The probability for integer value  $x$  in a Poisson distribution is  $e^{-\mu} \mu^x / x!$  for  $x \geq 0$ .

```
In[14]:= PDF[PoissonDistribution[μ]]
```

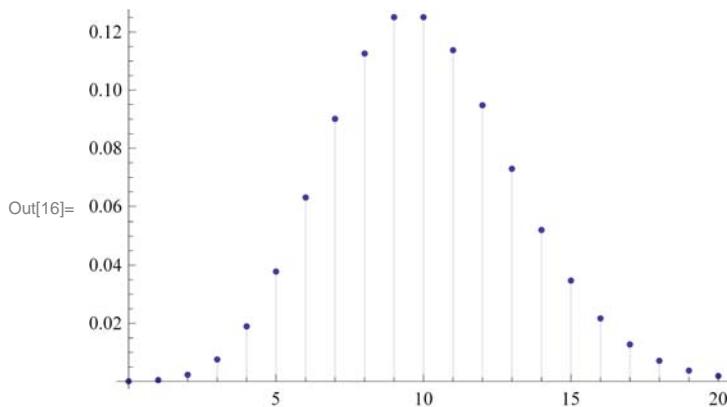
Out[14]= 
$$\frac{e^{-\mu} \mu^{\#\text{1}}}{\#\text{1}!}$$
 &

Probability density function:

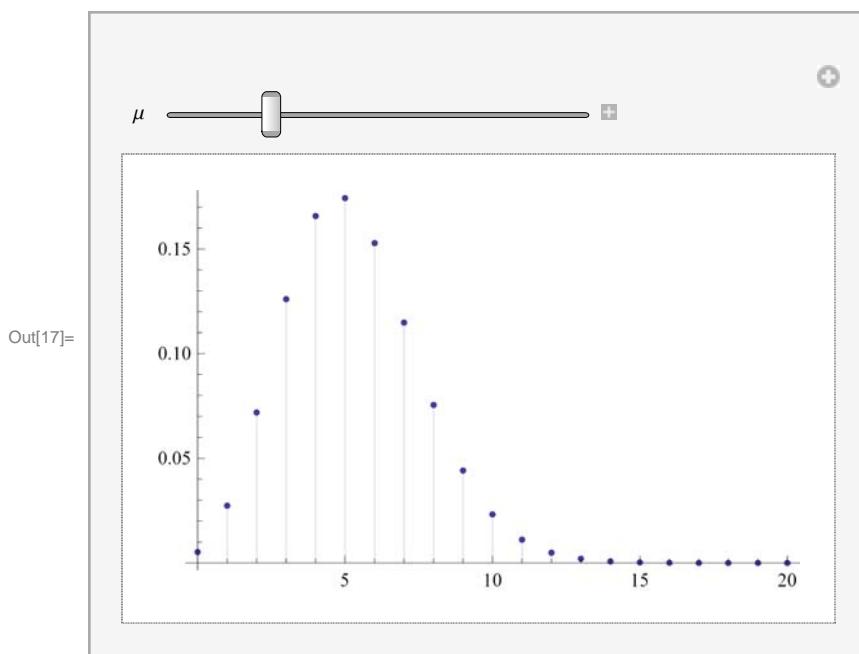
```
In[15]:= PDF[PoissonDistribution[μ], k]
```

Out[15]= 
$$\frac{e^{-\mu} \mu^k}{k!}$$

```
In[16]:= ListPlot[Table[{k, PDF[PoissonDistribution[10], k]}, {k, 0, 20}], Filling -> Axis]
```



```
In[17]:= Manipulate[ListPlot[Table[{k, PDF[PoissonDistribution[μ], k]}, {k, 0, 20}], Filling -> Axis], {μ, 1, 20}]
```



### BinomialDistribution[n, p]

represents a binomial distribution with  $n$  trials and success probability  $p$ .

The probability for value  $x$  in a binomial distribution is  $\binom{n}{x} p^x (1-p)^{n-x}$  for integers from 0 to  $n$

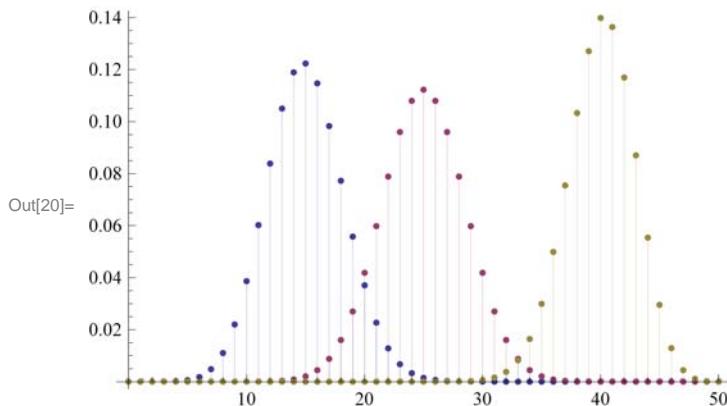
Mean and variance of a binomial distribution and the probability density function:

```
In[18]:= Mean[BinomialDistribution[n, p]]
Variance[BinomialDistribution[n, p]]
```

```
Out[18]= n p
```

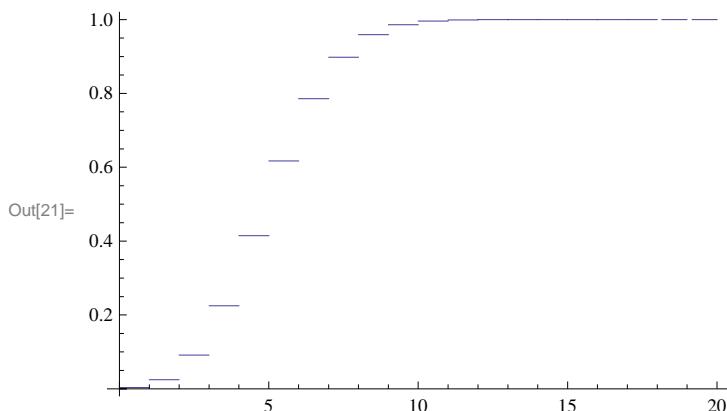
```
Out[19]= n (1 - p) p
```

```
In[20]:= ListPlot[Table[{k, PDF[BinomialDistribution[50, p], k]}, {p, {0.3, 0.5, 0.8}}, {k, 0, 50}], Filling -> Axis]
```



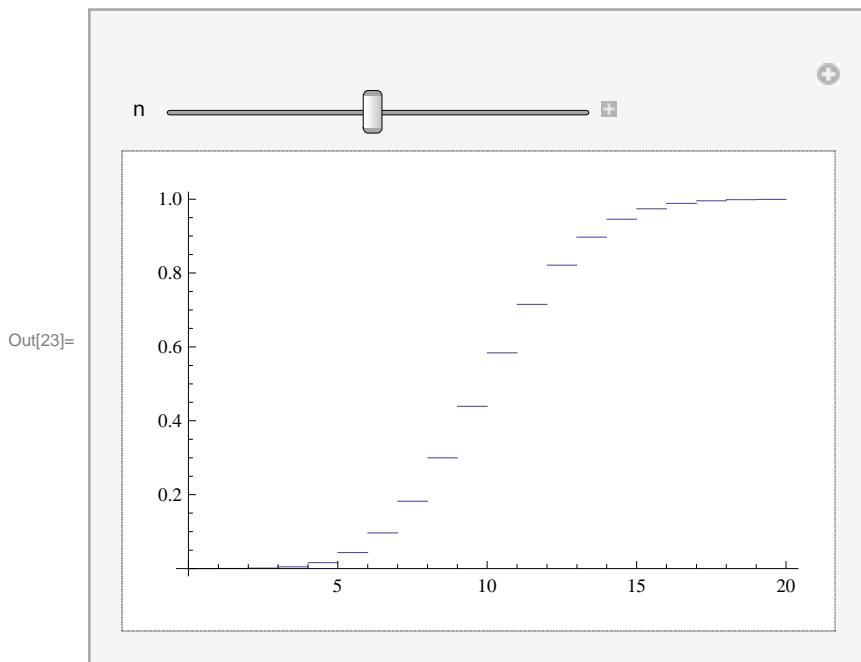
Plot the cumulative distribution function of a binomial distribution and the density functions of binomial random variables are highly concentrated about their means:

```
In[21]:= Plot[CDF[BinomialDistribution[20, 1/4], k], {k, 0, 20}]
ArrayPlot[Table[PDF[BinomialDistribution[n, 0.5], k], {k, 0, 30}, {n, 1, 60}]]
```



Out[22]=

```
In[23]:= Manipulate[Plot[CDF[BinomialDistribution[n, 1/4], k], {k, 0, 20}], {n, 2, 80, 2}]
```

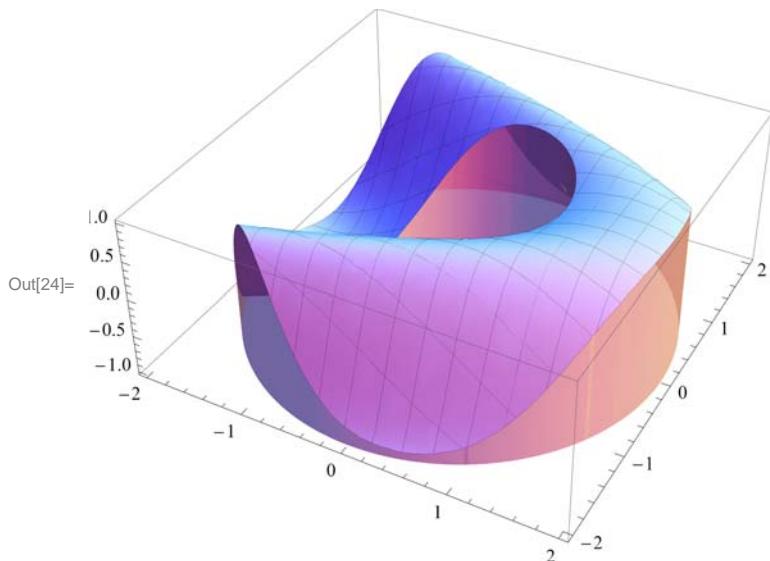


## RegionFunction

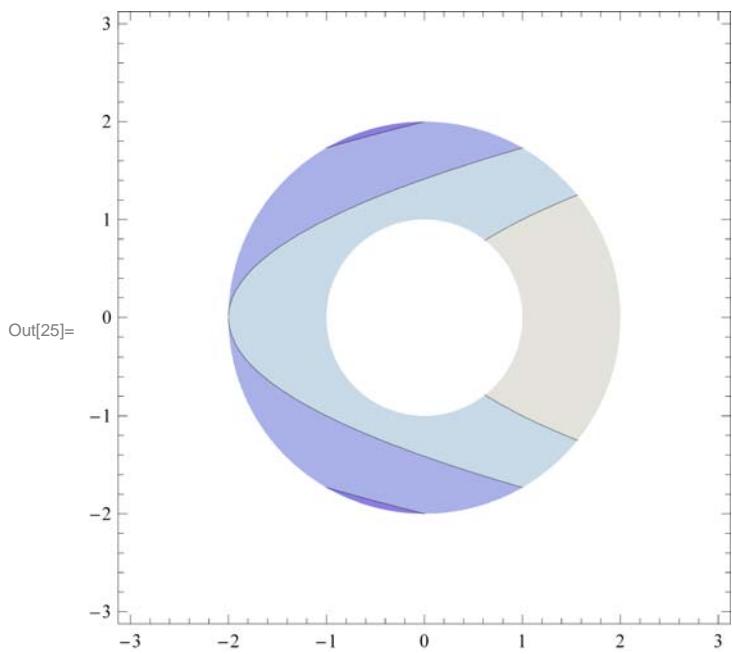
is an option for plotting functions which specifies the region to include in the plot drawn.

The setting `RegionFunction -> r` specifies that a point should be included in the region when `r[args]` yields True.

```
In[24]:= Plot3D[Sin[x + y^2], {x, -2, 2}, {y, -2, 2}, RegionFunction -> (1 < #1^2 + #2^2 < 4 &),
  Filling -> Bottom, FillingStyle -> Opacity[0.7], Mesh -> True]
```



```
In[25]:= ContourPlot[x - y^2, {x, -3, 3}, {y, -3, 3}, RegionFunction -> (1 < #1^2 + #2^2 < 4 &)]
```



```
In[26]:= Manipulate[Plot3D[Sin[a*x + b*y^2], {x, -2, 2}, {y, -2, 2}, RegionFunction -> (1 < #1^2 + #2^2 < 4 &), Filling -> Bottom, FillingStyle -> Opacity[0.7], Mesh -> True], {a, 0, 1}, {b, 2, 10}]
```

